## UniversidadeVigo



IDENTIFYING DATA
Mathematics: Calculus II

| Subject | Mathematics: Calculus II |
| :---: | :---: |
| Code | V09G310V01204 |
| Study programme | (*)Grao en Enxeñaría dos Recursos Mineiros e Enerxéticos |
| Descriptors | ECTS Credits Choose $\quad$ Year ${ }^{\text {a }}$ Quadmester |
|  |  |
| Teaching language | Spanish |
| Department |  |
| Coordinator | Álvarez Vázquez, Lino José |
| Lecturers | Álvarez Vázquez, Lino José <br> Martínez Varela, Áurea María |
| E-mail | lino@dma.uvigo.es |
| Web | http://faitic.uvigo.es |
| General description | In the subject of Calculus II of the Degree in Engineering of the Mining and Energetic Resources provides basic and common training to the branch of the engineering. Such and how features in the memory of the degree, after finalizing the subject the student will have to be able to formulate, resolve and interpret mathematically own problems of the engineering. Stop this, when surpassing the subject, will owe to know calculate integrals of functions of an and of varied variables, know his meaning and dominate the basic numerical methods of approximation of integrals. On the other hand, it has to be used with the handle and resolution of differential equations of first order and upper. All these contents are relevant for varied subjects that owes to study simultaneously or later in the qualifications. |


| Competencies |
| :--- |
| Code |
| C1 |
| C7 |
| C9 |
| D1 |
| D4 |
| D10 |


| Learning outcomes | Training and Learning <br> Results |  |
| :--- | :---: | :---: |
| Expected results from this subject | C1 | D1 |
|  |  | D4 |
| The objective that pursues this subject is that the student purchase the dominance of the basic | C1 |  |
| techniques of the integral calculation and his applications. This subject expects that the students | C7 | D5 |
| learn to: | C9 | D10 |
| - Comprise the basic bases of the theory of the integration of functions of an and several variables. |  |  |
| - Handle the elementary techniques of integration of ordinary differential equations. |  |  |

## Contents

Topic

1. Integral calculation of functions of one variable.

Generalities: The integral of Riemann. Integrable functions. Main theorem of the integral calculation. Theorem of the mean value. Rule of Barrow. Calculation of primitives: integration by parts and change of variable. Improper integrals.
2. Numerical methods of integration in R.
3. Integral calculation of functions of several variables.
4. Ordinary differential equations.

Formulas of Quadrature of polynomial type. Properties. Error of interpolation. Particular cases: Poncelet, Trapece and Simpson. Formulas of quadrature compound.
Double and triple integrals in elementary regions. Change of the order of integration. Change of variable. Polar coordinates. Cylindrical and spherical coordinates.
Generalities on ordinary differential equations. Concept of solution. First order equations. Existence and uniqueness of solution. Autonomous equations. Equations in separate variables. Homogeneous equations Exact equations. Linear equations. Families of curves: orthogonal trajectories.
5. Ordinary differential equations of upper order. Differential equations of second order and upper order. Linear equations homogeneous and non-homogeneous. Linear equations with constant coefficients. Method of indeterminate coefficients. Method of variation of parameters. Equation of Cauchy-Euler.
6. Numerical methods for ordinary differential equations.

Methods for problems of initial value: methods of one step, methods multistep, methods predictor-corrector. Methods for boundary problems: Methods of shot, methods of finite differences.
7. Introduction to the partial derivative equations. Classification: elliptic, hyperbolic and parabolic equations. Problems with boundary values and problems of initial value. Examples: equation of Laplace, heat equation and wave equation.

| Planning | Class hours | Hours outside the <br> classroom | Total hours |
| :--- | :--- | :--- | :--- |
| Master Session | 30 | 60 | 90 |
| Troubleshooting and / or exercises | 10 | 20 | 30 |
| Laboratory practises | 5 | 8.75 | 13.75 |
| Troubleshooting and / or exercises | 5 | 8.75 | 13.75 |
| Long answer tests and development | 2.5 | 0 | 2.5 |

*The information in the planning table is for guidance only and does not take into account the heterogeneity of the students.

| Methodologies | Description |
| :--- | :--- |
| The professor will expose in this type of kinds the theoretical contents of the subject. |  |
| Troubleshooting and / or In these hours of work the professor will resolve problems of each of the subjects and will enter new <br> exercises <br> methods of resolution no contents in the master sessions from a practical point of view. The <br> student also will owe to resolve problems proposed pole professor with the objective to apply the <br> knowledges purchased. |  |
| In these practices will use the tool computing MATLAB (or another similar) to study the numerical <br> methods of approximation of integrals and of resolution of ordinary differential equations described <br> in units 2 and 6. |  |
| Laboratory practises |  |
| Personalized attention | Description |
| Troubleshooting and / or | The professor will attend personally the doubts and queries of the students. Will attend doubts <br> so much of presence form, especially in the classes of problems and laboratories, as of non- <br> personal form by means of the platform Faitic. |
| Laboratory practises | The professor will attend personally the doubts and queries of the students. Will attend doubts <br> so much of presence form, especially in the classes of problems and laboratories, as of non- <br> personal form by means of the platform Faitic. |
| Master Session | The professor will attend personally the doubts and queries of the students. Will attend doubts <br> so much of presence form, especially in the classes of problems and laboratories, as of non- <br> personal form by means of the platform Faitic. |


| Assessment | Description | QualificationTraining <br> and <br> Learning <br> Results |
| :---: | :---: | :---: |


| Troubleshooting and or exercises | The evaluation will be preferably continuous. The student, in the first weeks of kind, will deliver to the teaching staff of the subject a form to enrol in this type of evaluation. Once expressed his I wish to by writing of not taking part, no longer will be able to gave of high of the continuous evaluation. The continuous evaluation features of the proofs that detail the continuation and in the that the student will resolve, along the 10 practices of laboratory, problems and exercises of the are afraid indicate in the following points: <br> * Four sessions of problems of an hour: <br> First session: Subject 1 (practical of the week 2) <br> Second session: Subject 3 (practical of the week 5) <br> Third session: Subject 4 (practical of the week 7) <br> Fourth session: Subject 5 (practical of the week 9) <br> * Two sessions of laboratory of half hour: <br> First session: Subject 2 (practical of the week 3) <br> Second session: Subject 6 (practical of the week 10) <br> These six proofs sum a $30 \%$ of the note having each a weight of a $5 \%$. <br> Learning outcomes: Comprise the basic bases of the theory of the integration of functions of an and several variables, and handle the elementary techniques of integration of ordinary differential equations. | 30 | C1 C7 C9 |  |
| :---: | :---: | :---: | :---: | :---: |
| Long answer tests and development | This proof is the final examination of the continuous evaluation, that will be done once finished the classes, with one weigh of $70 \%$ of the note, in the dates fixed by the Together of School (what can be consulted in the page web of the Centre). <br> Learning outcomes: Comprise the basic bases of the theory of the integration of functions of an and several variables, and handle the elementary techniques of integration of ordinary differential equations. | 70 | C1 C7 C9 | D1 <br> D4 <br> D5 <br> D10 |
| Other comments on the Evaluation |  |  |  |  |
| Sources of information |  |  |  |  |
| J. Stewart, Cálculo: Conceptos y contextos, Thomson, |  |  |  |  |
| E. Marsden - A.J. Tromba, Cálculo vectorial, Pearson-Addison, |  |  |  |  |
| D.G. Zill - M.R. Cullen, Matemáticas avanzadas para ingeniería: Ecuaciones diferenciales, McGraw[Hill, |  |  |  |  |
| A. Quarteroni - F. Saleri, Cálculo científico con Matlab y Octave, Springer, |  |  |  |  |

## Recommendations

Subjects that are recommended to be taken simultaneously
IT: Statistics/V09G290V01203
Subjects that it is recommended to have taken before
Mathematics: Linear algebra/V09G290V01103
Mathematics: Calculus I/V09G290V01104

