# Universida<sub>de</sub>Vigo

Subject Guide 2023 / 2024

IDENTIFYII	NG DATA				
<b>Mathemat</b>	ics: Linear algebra				
Subject	Mathematics: Linear				
	algebra				
Code	V05G306V01102				
Study	Bachelor Degree in				
programme	Telecommunication				
	Technologies				
	Engineering (BTTE)				
Descriptors	ECTS Credits		Choose	Year	Quadmester
	6		Basic education	1st	1st
Teaching	Spanish				
language					
Department	-				
Coordinator	Martín Méndez, Alberto Lucio				
Lecturers	Bajo Palacio, Ignacio				
	Calvo Ruibal, Natividad				
	Martín Méndez, Alberto Lucio				
E-mail	amartin@dma.uvigo.es				
Web	http://moovi.uvigo.gal/				
General	The subject Linear Algebra is taught in the first four-month period of the first course of the Grado en Ingeniería				
description	de Tecnologías de Telecomunicación, wit				
•	of the complex numbers, systems of line				
	introduction to the fundamental concepts of Vector Spaces which will be needed in later subjects. Special				
	attention will be paid to the applications				•

# **Training and Learning Results**

Code

- B3 CG3: The knowledge of basic subjects and technologies that enables the student to learn new methods and technologies, as well as to give him great versatility to confront and adapt to new situations
- B4 CG4: The ability to solve problems with initiative, to make creative decisions and to communicate and transmit knowledge and skills, understanding the ethical and professional responsibility of the Technical Telecommunication Engineer activity.
- C1 CE1/FB1: The ability to solve mathematical problems in Engineering. The aptitude to apply knowledge about linear algebra, geometry, differential geometry, differential and integral calculus, differential and partial differential equations; numerical methods, numerical algorithms, statistics and optimization
- D2 CT2 Understanding Engineering within a framework of sustainable development.
- D3 CT3 Awareness of the need for long-life training and continuous quality improvement, showing a flexible, open and ethical attitude toward different opinions and situations, particularly on non-discrimination based on sex, race or religion, as well as respect for fundamental rights, accessibility, etc.

Expected results from this subject				
Expected results from this subject		Training and Learning		
		Resu	ılts	
Skill development the basic operations of matrix algebra.	В3	C1	D2	
	B4		D3	
Knowledge of numerical methods for solving systems of linear equations and knowledge of the	B3		D3	
basic concepts involving vector spaces and linear maps.				
Knowledge of the properties of vector spaces with inner product.		C1	,	
Skill development some applications of linear algebra: the method of least squares, singular value decomposition and classification of quadratic forms	В3	C1	D3	
To know the arithmetic of complex numbers.	В3	C1	D2	
	B4		D3	

#### **Contents**

Topic	
Topic 1. Complex numbers.	Operations with complex numbers. Geometric concepts associated with complex numbers. Euler's formula and its consequences.
Topic 2. Matrices and determinants.	Matrix operations: addition, scalar multiplication and product of matrices. Matrix inverse. Block matrices. Determinants.
Topic 3. Systems of linear equations.	Systems of linear equations. Elementary row operations and Gauss method. Numerical methods for systems of linear equations.
Topic 4. Vector spaces and linear transformations.	Linear independence. Subspaces. Basis. Dimension. Rank of a system of vectors. Introduction to linear transformations. Matrix of a linear transformation.
Topic 5. Matrix diagonalization.	Eigenvalues and eigenvectors. Eigenspace. Matrix diagonalization and diagonalizable matrices.
Topic 6. Orthogonallity.	Real Euclidean inner product. Complex Hermitian inner product. Orthogonallity. Gram-Schmidt. Unitary Diagonalization. Singular value decomposition. Matrix rank reduction. The method of least squares. Quadratic forms.

Planning			
	Class hours	Hours outside the classroom	Total hours
Laboratory practical	2	2	4
Lecturing	46	69	115
Problem solving	9	9	18
Problem and/or exercise solving	3	5	8
Essay questions exam	3	2	5
	3 3	5 2	8 5

<sup>\*</sup>The information in the planning table is for guidance only and does not take into account the heterogeneity of the students.

Methodologies	
	Description
Laboratory practical	Solving assigned exercises and model problems. Use of the computer tool MATLAB.
	Through this methodology the competences CG3, CG4, CE1, CT2 and CT3 are developed.
Lecturing	Explanation and development by the teacher of the contents of the various topics in the syllabus.
	Through this methodology the competences CG3, CE1 and CT3 are developed.
Problem solving	Resolution by part of the professor of suitable exercises adapted to each topic.
	The students will also have to take part in the resolution of exercises in order to strengthen their knowledge.
	Through this methodology the competences CG3, CG4, CE1, CT2 and CT3 are developed.

Personalized assistance		
Methodologies	Description	
Problem solving	Personalized tutoring will be available from all the teachers of the subject.	
Laboratory practical	Personalized tutoring will be available from all the teachers of the subject.	
Lecturing	Personalized tutoring will be available from all the teachers of the subject.	
Tests	Description	
Problem and/or exercise solvin	g Personalized attention will be available for assistance in the revision of tests and exams.	

Assessment	
Description	Qualification Training and
·	Learning Results

Problem and/or exercise solving	Continuous evaluation consists in three tests to be given in the class hour. The planning will be the following:  1. Exam of topic 1 and 2.  2. Exam of topic 3 and 4.  3. Exam of topic 5 and 6.	60	B3 B4	C1
	Each test will have a weight of 20% in the final grade.			
	The total weight of the continuous evaluation in the final grade will therefore be of 60%.			
	The planning of the different intermediate evaluation tests will be approved in an Academic Commission of Degree and it will be available at the beginning of the semester.			
Essay questions exam	A written exam, with a maximum duration of three hours, of topics 1, 2, 3, 4, 5 and 6 at the end of the semester in date, time and venue determined in the official exams calendar of the School.	40	B3 B4	C1

#### Other comments on the Evaluation

#### **Ordinary assessment:**

#### **Continuous assessment:**

The final grade is calculated by the formula:

$$M = (2 \times (E1 + E2 + E3) + 4 \times EF) / 10$$

where E1, E2 and E3 are the points, in a scale 0 to 10, obtained in the three tests of the continuous evaluation and where EF represents the points, in a scale 0 to 10, obtained in the final exam. Before doing each test, the procedure and date of revising the grading of that test will be announced. After the test, the grades will be announced in a reasonable amout of time. If a student, for any circumstance, cannot attend a particular test on the date for which it is scheduled, he or she will miss that test and it will not be repeated.

The points obtained in the tests of continuous evaluation will be valid only for the academic year in which they are obtained.

It will be considered that a student has chosen to follow the continuous evaluation if he takes the second exam, that is, that of topics 3 and 4.

#### Global assessment:

The students who do not choose to be graded by continuous evaluation, will be graded by means of a final exam of all the topics of the subject. This exam will be graded in a scale of 10 points and the passing grade cutoff will be 5.

#### **Extraordinary exam:**

The students who at the end of the semester do not obtain a passing grade will have the opprtunity of writing a second final exam on date, time and venue determined in the official exams calendar of the School. This exam will cover topics 1, 2, 3, 4, 5 and 6 and it will be graded in a scale of 10 points and the passing grade cutoff will be 5.

**Remark:** During the exam correction period some students could be contacted by phone or telematically by the teacher to clarify aspects of their answers; in that case, such answers may have an impact on the exam grade.

#### "No presentado":

A student will obtain a grade of "No Presentado" in the ordinary exam if that student did not attend neither the continuous evaluation nor the final exam.

A student will obtain a grade of "No Presentado" in the second edition of the final grades if and only if that student obtained "No Presentado" in the first call and did not attend the second final exam.

#### **End-of-program exam:**

The students which attend the end-of-program exam will write an exam covering topics 1, 2, 3, 4, 5 and 6 which will be graded in a scale of 10 points and the passing grade cutoff will be 5.

#### **Ethical Behavior:**

It is expected a correct and ethical behavior of all students in all written tests and exams, which are meant to truly reflect

the knowledge and abilities attained by each studen. Any unethical behavior detected in a particular test (such as copying or using prohibited material) will result in a grading of 0 in that test and the issue of the corresponding report for the School Director's Office.

# Sources of information

#### **Basic Bibliography**

D. Poole, **Álgebra lineal: Una introducción moderna**, 2º, Cengage Learning Editores S.A., 2006

L. Merino; E. Santos, **Álgebra lineal con métodos elementales**, 1ª, Paraninfo, 2006

J. de Burgos, **Álgebra lineal y geometría cartesiana**, 2ª, McGraw-Hill/Interamericana de España, S. A. U., 2000

# **Complementary Bibliography**

D. C. Lay, **Álgebra lineal y sus aplicaciones**, 3ª, Pearson Educación, 2007

#### Recommendations

#### Subjects that continue the syllabus

Physics: Analysis of Linear Circuits/V05G301V01108

Mathematics: Calculus 2/V05G301V01106 Physics: Fields and Waves/V05G301V01202

# Subjects that are recommended to be taken simultaneously

Mathematics: Calculus 1/V05G301V01101